

IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

UTILITY APPLICATION AND FEE TRANSMITTAL (1.53(b))

COMMISSIONER FOR PATENTS
BOX PATENT APPLICATION
Washington, D.C. 20231

Sir:

Transmitted herewith for filing is the patent application of

Inventor(s) names and addresses:

- (1) Gerrit Bleumer
c/o Francotyp-Postalia
Trifweg 21-26, D-16547
Birkenwerder, GERMANY

(2)

☐ Additional inventors are listed on a separate sheet

For: METHOD FOR GENERATING MANY-TIME RESTRICTIVE BLIND SIGNATURES

Enclosed Are:

- 19 page(s) of specification
1 page(s) of Abstract
2 page(s) of claims
1 sheets of ☒ Formal ☐ Informal drawings

2 page(s) of Declaration and Power of Attorney

- ☒ Unsigned
☐ Newly Executed
☐ Copy from prior application
☐ Deletion of inventors including Signed Statement under 37 C.F.R. §1.63(d)(2)

☒ **Incorporation by Reference:**

- ☒ The entire disclosure of the prior application, from which a copy of the combined Declaration and Power of Attorney is supplied herein, is considered as being part of the disclosure of the accompanying application and is incorporated herein by reference.

- ☐ Microfiche Computer Program (Appendix)
- ☐ page(s) of Sequence Listing
- ☐ computer readable disk containing Sequence Listing
- ☐ Statement under 37 C.F.R. §1.821(f) that computer and paper copies of the Sequence Listing are the same
- ☐ Assignment Papers (assignment cover sheet and assignment documents)
- ☐ A check in the amount of \$40.00 for recording the Assignment
- ☐ Charge the Assignment Recordation Fee to Deposit Account No. 13-4503, Order No. _____
- ☐ Assignment Papers filed in the parent application Serial No. _____
- ☐ Certification of chain of title pursuant to 37 C.F.R. §3.73(b)
- ☐ Priority is claimed under 35 U.S.C. §119 for:
Application No(s). _____, filed _____, in _____ (country).
- ☐ Certified Copy of Priority Document(s) [_____]
- ☐ filed herewith
- ☐ filed in application Serial No. _____, filed _____.
- ☐ English translation document(s) [_____]
- ☐ filed herewith
- ☐ filed in application Serial No. _____, filed _____.
- ☒ Priority is claimed under 35 U.S.C. §119(e) for:
Provisional Application No. 60/161,062, filed October 25, 1999.
- ☐ Priority is claimed under 35 U.S.C. §120 for:
Application No(s). _____, filed _____, in _____.
- ☒ Information Disclosure Statement
- ☒ Copy of [26] cited references
- ☒ PTO Form-1449
- ☐ References cited in parent application Serial No. _____, filed _____.
- ☐ Preliminary Amendment
- ☒ Return receipt postcard (MPEP 503)
- ☐ This is a ☐ continuation ☐ divisional ☐ continuation-in-part of prior application serial no. _____, filed _____.
- ☐ Cancel in this application original claims _____ of the parent application before calculating the filing fee. (At least one original independent claim must be retained for filing purposes.)
- ☐ A Preliminary Amendment is enclosed. (Claims added by this Amendment have been properly numbered consecutively beginning with the number following the highest numbered original claim in the prior application).
- ☐ The status of the parent application is as follows:

☐ A Petition for Extension of Time and a Fee therefor has been or is being filed in the parent application to extend the term for action in the parent application until _____.

☐ A copy of the Petition for Extension of Time in the co-pending parent application is attached.

☐ No Petition for Extension of Time and Fee therefor are necessary in the co-pending parent application.

☐ Please abandon the parent application at a time while the parent application is pending or at a time when the petition for extension of time in that application is granted and while this application is pending has been granted a filing date, so as to make this application co-pending.

☐ Transfer the drawing(s) from the parent application to this application

☐ Amend the specification by inserting before the first line the sentence:
This is a continuation of co-pending application Serial No. _____, filed _____.

I. CALCULATION OF APPLICATION FEE				
	Number Filed	Number Extra	Rate	Basic Fee \$710.00/355.00
Total Claims	13- 20 =	0x	\$18.00/\$9.00	\$ 0.00
Independent Claims	3- 3 =	0x	\$80.00/\$40.00	\$ 0.00
<input type="checkbox"/> Multiple Dependent Claims		If marked, add fee of \$270.00 (\$135.00)		\$ 0.00
TOTAL:				\$ 710.00

☐ A statement claiming small entity status is attached or has been filed in the above-identified parent application and its benefit under 37 C.F.R. §1.28(a) is hereby claimed. Reduced fees under 37 C.F.R. §1.9 (f) paid herewith \$_____.

☐ A check in the amount of \$ _____ in payment of the application filing fees is attached.

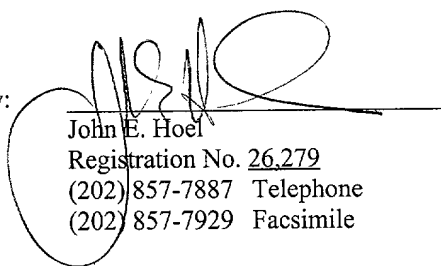
☐ Charge fee to Deposit Account No. 13-4500 Order No. _____. A DUPLICATE COPY OF THIS SHEET IS ATTACHED.

- ☒ The Commissioner is hereby authorized to charge any additional fees which may be required for filing this application pursuant to 37 CFR §1.16, including all extension of time fees pursuant to 37 C.F.R. § 1.17 for maintaining copendency with the parent application, or credit any overpayment to Deposit Account No. 13-4503 Order No. 2455-4581US1. A DUPLICATE COPY OF THIS SHEET IS ATTACHED.

Respectfully submitted,
MORGAN & FINNEGAN, L.L.P.

Dated: Oct 23, 2000

By:


John E. Hoel

Registration No. 26,279

(202) 857-7887 Telephone

(202) 857-7929 Facsimile

CORRESPONDENCE ADDRESS:

MORGAN & FINNEGAN, L.L.P.
345 Park Avenue
New York, NY 10154



TITLE OF THE INVENTION**Method For Generating Many-Time Restrictive Blind Signatures**

5 Inventor: Gerrit Bleumer

RELATED APPLICATIONS:

10 This application is based on U.S. Provisional Serial No. 60/161,062, filed October 25, 1999.

BACKGROUND OF THE INVENTION

15

1. Field of the Invention

The invention disclosed broadly relates to cryptography and more particularly relates to digital signature methods.

20

In contrast to conventional digital signature schemes, blind signature schemes allow the recipient to obtain signatures for messages that the signer does not learn. If the recipient can get only one signed message from each execution of the signing operation by the signer, then the blind signature scheme is called *one-time*, otherwise it is called *many-time*. Many-time blind signatures have been used to build untraceable tickets, called *credentials*. Such tickets can be issued by one organization and verified by another. Each customer uses different pseudonyms with each organization and a ticket is simply a blind signature for a customer pseudonym. The blinding property allows one to use different pseudonyms for issuing and showing a ticket. Even if all organizations collude, they cannot trace which tickets belong to which customers. One-time blind signatures have been used to build practical offline and online untraceable electronic cash schemes, where the issuing organizations are banks, the recipients are merchants and the tickets can be used only once. Most electronic cash schemes based on blind

30

signatures use the one-time form, mainly to avoid the problem of multiple copies of the same electronic coin.

For offline untraceable electronic cash, double spending of coins should be detectable after the fact, so that double spenders are identifiable if and only if they use a coin more than once. This problem has been addressed by using restrictive one-time blind signatures. The customer's identity is embedded into her pseudonyms in such a way that it is revealed if and only if she double spends. A general blind signature scheme would allow a customer to also obtain coins for pseudonyms of other customers or for pseudonyms that are not assigned to anyone. In contrast, restrictive blind signature schemes guarantee that customers form their pseudonyms in a way that preserves the customer's identity, which the signer has encoded into each issued pseudonym.

A related application area is untraceable membership cards, which can be stored in palmtops, smartcards, etc. Owners may use their membership cards online or offline, arbitrarily often, and in an untraceable way, i.e., several uses of the same card cannot be linked by the respective verifiers. However, issuers of membership cards require that membership cards can be used only by their owners, not by other individuals, even if the owners wish to lend their membership cards away. Purely cryptographic solutions to this problem cannot exist because whether a membership card is actually used by its owner or someone else, is not distinguishable by cryptographic means. It has been suggested to use a wallet-with-observer architecture, where every user has a personal device (wallet) that is in part controlled by an implanted tamper resistant security module (observer). The observers can be equipped with a biometric sensor which is a sufficiently powerful hardware basis for the problem at hand. The prior art relies heavily on the tamper resistance of observers, because if an attacker breaks his observer he can

not only lend his own membership cards to other individuals, but he can also forge new membership cards. Another approach relies on the tamper resistance of only observers with respect to transferability of membership cards. Attackers who break their observers can at most pool all the membership cards they already have, but cannot produce new ones. The approach
 5 includes a "cascade" signature scheme which has not been implemented.

What is needed in the prior art is a restrictive blind signature scheme that allows a recipient to obtain signatures for arbitrarily many (correctly formed) messages after only one interaction with the signer.

10 **SUMMARY OF THE INVENTION**

A multiple use ticket generating method is disclosed which enables a recipient to obtain signatures for arbitrarily many (correctly formed) messages after only one interaction with the signer. The method provides a blind signature in a ticket, the signature having a multiple use with a built-in expiration. Then, the method develops a blinding value for the signature in a
 15 reproducible computation using a seed key substantially known only to the issuer of the ticket. The method implements a new class of man-time restrictive blind signature schemes almost as efficiently as do previous one-time restrictive blind signature methods.

The resulting ticket can be in the form of an electronic personal ticket, such as a season ticket for sporting events. Other forms for the ticket can include a personal license, such as a
 20 personal driver's license. The ticket has the property of being untraceable and has the advantage that the signature does not require an interactive signing protocol.

DESCRIPTION OF THE FIGURES

Figure 1 shows a method for producing a signature.

5 Figure 2 shows a method for transforming a signature.

DESCRIPTION OF THE PREFERRED EMBODIMENTS

10 An efficient implementation of a many-time restrictive blind signature scheme is disclosed. It uses no hash function, is about as efficient as previous one-time restrictive blind signature methods, and its security rests on a similar assumption as that of the ElGamal signature scheme. Applications for the new signature scheme are untraceable offline personal tickets, e.g., monthly season tickets, driver's licenses, or coupons that can be used multiple times until they
 15 expire. A computer system for carrying out the method of the invention is a standard general purpose data processor that includes a random access memory to store the program embodiment of the invention and a central processor to execute the instructions in the program embodiment. The computer system is connected to a network to generate and circulate untraceable tickets, licenses, or coupons that can be used multiple times until they expire.

Definitions

A definition follows of many-time restrictive blind signatures. The formalization of restrictiveness follows ideas of Brands [B93], Franklin and Yung [FY93] and Pfitzmann and Sadeghi [PS99].

Definition 1 (Many-time restrictive blind signature).

25 A many-time restrictive blind signature scheme consists of a security parameter $k \in \mathbb{IN}$, a signing key space X , a verifying key space Y , a message space M , a signature space Σ , a blinder space Ω , a witness space W , and a relation $make \subseteq M \times W$. Also included is an equivalence

relation on W (equivalent witnesses $v, w \in W$ are denoted $v \equiv w$), more precisely, there are families of all these domains indexed by the security parameter k . If $(w, m) \in \text{make}$ then we say that witness w *makes* message m . At system setup time, a particular security parameter is chosen and from then on, only one instance of each domain is used. Also included are two probabilistic protocol algorithms *gen*, *sign*, a probabilistic protocol *trans* of two participants Bob and Verifier,

5 and a deterministic algorithm *verify*, which are declared as follows:

$$\begin{array}{ll} (x, y) \leftarrow \text{gen}(k) & \sigma \leftarrow \text{sign}(x, m) \\ (m', \sigma') \leftarrow \text{trans}(y, m, \sigma, w) & \text{acc} \leftarrow \text{verify}(y, m, \sigma) \end{array}$$

All of them are efficiently computable. Given a security parameter k , the key generating algorithm *gen* returns a pair of a private signing key $x \in X$ and a public verification key $y \in Y$.

10 The algorithm *sign* takes as input a signing key $x \in X$ and a message $m \in M$. It returns a signature $\sigma \in \Sigma$. The protocol *trans* takes as input for both Bob and the Verifier a verification key y , and only for Bob a message m , a signature σ and a blinder ω . After the protocol, both Bob and the Verifier return the same message m' and signature σ' . The algorithm *verify* takes as

15 input a public key y , a message $m \in M$ and a signature $\sigma \in \Sigma$ and returns a Boolean value *acc*. If *verify* (y, m, σ) returns True then the signature σ is called *valid* for m with respect to public key y , or the pair (m, σ) is *valid* for y .

EFFECTIVENESS: For every security parameter k , every key pair $(x, y) \leftarrow \text{gen}(k)$, and every message $m \in M$ the algorithm *sign* (x, m) produces a valid signature σ for m . For all

20 inputs as above, every blinder $\omega \in \Omega$ and every signature $\sigma \in \Sigma$ valid for m the algorithm *trans* (y, m, σ, ω) returns a valid signature σ' for m' .

RESTRICTIVENESS with respect to *make* and \equiv : Every polynomial-time attacker who

(i) obtains valid signatures σ_i ($i = 0 \dots n$) from the signer for respective messages m_i of his

(adaptive) choice. The choice of each message he asks to be signed may depend on all messages previously chosen and the corresponding responses by the signer. The attacker also (ii) comes up with a new message m' and signature σ' and (iii) delivers $n + 1$ witnesses $\omega_1, \omega_2, \dots, \omega_n, \omega'$ has only a negligible chance of achieving the following event: The signature σ' is valid for m' , the witnesses ω_i, ω' each match their messages m_i, m' and the witness ω' is not equivalent to any of the witnesses ω_i if any.

UNLINKABILITY: Let $(m, \sigma), (m', \sigma')$ be two pairs valid with respect to y . Then for each internal choice r_V of the Verifier in *trans*, there is a unique blinder $\omega \in \Omega$ and a unique internal choice, (i.e., a sequence of random bits used by a probabilistic algorithm) r_B for Bob in algorithm *trans*, such that the execution of *trans* (y, m, σ, ω) with internal choices r_B, r_V returns (m', σ') .

Note that previous one-time blind signature schemes use an interactive signing protocol from which the recipient gets a message and signature that he can later show to a verifier without interaction. Many-time blind signature schemes use a non-interactive signing protocol from which the recipient gets a message and signature that he can later transform and thereby show to many verifiers.

3 The Rust Signature Scheme

The proposed many-time blind signature scheme is referred to here as "RUST". The standard discrete log setting is adopted. Let p be a large prime, q be a large prime divisor of $p - 1$. Typically, p and q will be chosen about 1024 bit and 160 bit long, respectively [O99]. Then Z_p^* has a unique subgroup G_q of order q and since Z_p^* is cyclic, so is G_q . Let g, g_1 be generators of G_q that are chosen uniformly at random.

The private and public key spaces are ZZ_q and G_q , respectively. The message space is $M = G_q^* \setminus \{1\}$, where G_q^* is G_q except all members that disappear modulo q . The signature space is $\Sigma = G_q^* \times ZZ_q \times ZZ_q^*$, the space of blinders is $\Omega = ZZ_q^*$, the witness space is $W = ZZ_q$, the making relation is

$$5 \quad make = \{(m, \omega) \in M \times W \mid m = g_1^\omega \bmod p\},$$

and any two witnesses are equivalent, i.e., $\forall v, w \in W: v \equiv w$. Key generation is by choosing a signing key $x \in X$ uniformly at random and computing the corresponding verification key $y = g^x \bmod p$.

A signature $(r, s, t) \in \Sigma$ (thus the name of the scheme) is *valid* for message $m \in M$ with respect to public key y if the following *equation* holds:

$$10 \quad verify(y, m, \sigma) = g^{r+s} = y^{m+t} m^{rs} r^{rt} \bmod p. \quad (1)$$

A pair (m, σ) is called *terminated* if $t = -m \bmod q$, otherwise it is called *fresh*.

3.1 Producing Signatures

Let the generator g , and a key pair (x, y) be setup as above. A signature for a given message $m \in M$ is constructed as shown in Figure 1:

One chooses $a, b \in_R ZZ_q$ uniformly at random such that $a+bm \neq -1 \pmod{q}$ in step (1) and computes the signature component r in step (2). If any of the values $r, r-mx$ or $(a+bm)rmx$ disappears modulo q , then the execution needs to be repeated from step (1). In step (3), the remaining signature values s, t are computed.

20 3.2 Transforming Signatures

Given a verification key y and a blinder $\omega \in \Omega$, a fresh pair $(m, (r, s, t)) \in M \times \Sigma$ of a message and a signature is transformed into another pair $(m', (r', s', t'))$. The blinder ω is required such that $m^\omega \bmod p \neq 0 \pmod{q}$ (see Figure 2): In step (1) through (5) Bob forms the new message m' and the signature component $r' = m^a r^b g^c y^d$ such that:

1. the exponents $b = \frac{rt}{m+t}d$ and $c = -\frac{a}{\omega m'} + d \frac{ms - \omega(r+s)m'}{\omega(m+t)m'} - \frac{1}{m'}$ are functions of a and d ,
2. the Verifier does not learn any information about Bob's input $m, (r, s, t)$,
3. even if Bob deviated from the protocol, he could not end up with some r' for which he has a representation with respect to m, r, g only, i.e., $d = 0$.

5 In detail, Bob chooses uniformly at random an auxiliary value $\alpha \in_R \mathbb{Z}\mathbb{Z}q$, and the Verifier chooses $d \in_R \mathbb{Z}\mathbb{Z}q$ (step (1)). Then Bob computes the output message $m' = m^\alpha \bmod p$ in step (2). Bob further computes the auxiliary values (β, γ) and the preliminary signature component r^* in step (3). After sending m', r^* to the Verifier, he obtains in return the Verifier's choice d in order to compute the signature component r' in step (5). So does the Verifier. Only
 10 in the case if d or r' disappears modulo q must the protocol be repeated from step (1). Next, Bob computes the exponents a, b according to step (6) and the signature components s', t' according to step (7). He finally sends the signature components s', t' to the Verifier. Figure 2 illustrates transforming a signature.

15 *Remark 2.* The RUST signature scheme ensures that signers always produce fresh pairs of messages and signatures and that only fresh pairs can be transformed. Note that if $t = -m \bmod q$ some quotients in *trans* were undefined. However, transformed pairs are always terminated, so that a Verifier cannot transform a pair further. This feature of RUST is not implied by restrictiveness (Definition 1).

20 The protocol *trans* can be made non-interactive if one is willing to rely on the obscurity of some hash function H as in the standard Fiat-Shamir technique [FS87]: Instead of sending m', r^* after step (3) and obtaining the Verifiers choice d in return, Bob can compute $d = H(y, m', r^*)$ after step (3) by himself. After step (7), Bob then sends m', r^*, s', t' to the Verifier. Finally, the Verifier checks in addition to the verification equation (1) whether $r' = (r^* y)^{H(y, m', r^*)} g^{-1/m'}$.

25 The witness equivalence used for the RUST signature scheme is degenerate in the sense that any two witnesses are equivalent. This is no weakness of the RUST signature scheme, but allows producing and transforming signatures quite efficiently. Note that Brands suggests to use his one-time restrictive blind signature scheme for offline e-cash [B93] with the same

degenerate witness equivalence (and function *make*). In offline e-cash, the price for the increased performance is computational instead of unconditional non-frameability. For many-time restrictive blind signatures, like the RUST scheme, signer identification by (more than one) signatures is no issue, and thus framing of signers is no issue either.

5 4. **Main Result**

In order to analyze the security of a proposed many-time restrictive blind signature scheme, referred to here as RUST, one needs the following two assumptions. These assumptions are not among the intensely investigated complexity theoretic assumptions like the discrete logarithm assumption [MOV97]. Nevertheless, they also underlie for example the ElGamal signature scheme and its derivatives without having been made explicit in previous work.

Assumption 1.

For some natural number $n \in \mathbb{N}$, let g_i ($i \in [1, n]$) be generators of G_q , and define the function

$$F_{g_1, g_2, \dots, g_n}(x_1, x_2, \dots, x_n) = \prod_{i=1}^n g_i^{x_i} \bmod p$$

that takes arguments $x = (x_1, x_2, \dots, x_n) \in \mathbb{Z}_q^n \setminus \{(0, 0, \dots, 0)\}$. Then the function

$$F_{g_1, g_2, \dots, g_n}(x) \bmod q$$

is an implementation of a random oracle [BR93]. (Note the difference of the moduli p and q !)

Assumption 2.

If at all, a polynomial-time attacker A can compute valid pairs of messages and signatures with respect to a given verification key y , but then only as follows:

- First pick a set of $n \geq 1$ generators h_1, \dots, h_n of G_q ,
- choose tuples $\mathbf{a}, \mathbf{b} \in \mathbb{Z}_q^n$,
- form the message $m' = F_{h_1, \dots, h_n}(\mathbf{a})$ and the signature component $r' = F_{h_1, \dots, h_n}(\mathbf{b})$,
- and finally compute the signature components s', t' .

Without loss of generality, the attacker can be assumed to pick the generators h_1, \dots, h_n such that he cannot feasibly find a representation of 1 with respect to h_1, \dots, h_n in G_q . Otherwise, he could represent at least one of the generators with respect to the others, and thus he could pick a proper subset of $\{h_1, \dots, h_n\}$ in the first step above, adapt the following steps accordingly and end up with the same result $(m', (r', s', t'))$.

A similar assumption has been used to reason about the security of ElGamal signatures [EG85], but those assumptions were left implicit.

Theorem 3. *Under assumptions A1 and A2, RUST is a many-time restrictive blind signature scheme.*

Proof. Check effectiveness, restrictiveness and blindness in turn.

Effectiveness of sign: Under Assumption A1, the probability to make a choice $a, b \in \mathbb{Z}_q$ such that any of the values $r, r - mx$ or $D \stackrel{\text{def}}{=} (a + bm)r + mx$ disappears modulo q is negligible and so is the probability to repeat step (2) of algorithm *sign*. In order to verify algorithm *sign* (see Figure 1), insert its output into the right hand side of verification equation (1):

$$\begin{aligned}
 y^{m+t} m^{ms} r^{rt} &= g^{x(m+t)} m^{ms} (m^a g^b)^{rt} \\
 &= g^{x(m+t) \frac{r-mx}{D}} m^{\frac{amr}{D}(mx-r)} m^{\frac{amr}{D}(r-mx)} g^{\frac{bmr}{D}(r-mx)} \\
 &= g^{\frac{mx}{D}((a+bm)r+mx+r-mx)} g^{\frac{bmr}{D}(r-mx)} \\
 &= g^{\frac{mr}{D}(a+bm+1) + \frac{mr}{D}(br-bmx)} \\
 &= g^{\frac{mr}{D}(ax+x+br)} \\
 &= g^{\frac{r}{D}(ar+amx+mx+bmr-ar)} \\
 &= g^{\frac{r}{D}(D+amx-ar)} \\
 &= g^{r + \frac{ar}{D}(mx-r)} \\
 &= g^{r+s} \pmod{p} .
 \end{aligned}$$

The signer produces fresh signatures because he chooses

$$t = m \frac{r - mx}{(a + bm)r + mx} \neq m(-1) = -m \pmod{q} \text{ according to the condition } a \neq bm + 1 \pmod{q} \text{ in}$$

step (1) of Figure 1. The signature components r and t do not disappear modulo q because of the loop condition in step (2).

- 5 **Effectiveness of trans:** The following verification is prepared by expressing Bob's signature components r' and s' in terms of Bobs input and his internal choices α , d and by using the definitions of β and γ according to step (3) of Figure 2:

$$r' = (r * y)^d g^{\frac{-1}{m'}} = (m^\alpha r^\beta g^\gamma y)^d g^{\frac{-1}{m'}} = m^{\alpha d} r^{\frac{rt}{m+r}d} g^{\frac{ms - \omega(r+s)m'}{\omega(m+t)m'}d - \frac{\alpha d}{\omega m'} - \frac{1}{m'}} y^d \quad (2)$$

$$s' = \frac{art - bms}{\omega rt} r' = \frac{r'}{\omega rt} \left(\alpha d r t - \frac{rt}{m+t} d m s \right) = d \frac{r'}{\omega} \left(\alpha - \frac{ms}{m+t} \right). \quad (3)$$

Under Assumption A1, the probability of choosing $a \in \mathbb{Z}\mathbb{Z}_q, d \in \mathbb{Z}\mathbb{Z}_q^*$, such that $r' = 0 \pmod{q}$ is negligible, and so is the probability of repeating after step (5). Next, insert the output $m', (r', s', t')$ of algorithm *trans* into the verification equation (1) and by inserting the expressions for $m' = m^\omega$ and r' according to equation (2):

$$\begin{aligned}
& y^{m'+t'} m'^{m's'} r'^{r't'} \\
&= m^{\frac{\omega m' a r t - b m s}{\omega r t}} \left(m^{\alpha d} r^{\frac{r t}{m+t} d} g^{\frac{m s - \omega(r+s)m'}{\omega(m+t)m'} d - \frac{\alpha d}{\omega m'} - \frac{1}{m'}} y^d \right)^{-r'm'} \\
&= m^{\frac{\omega m' r'}{\omega} \left(\alpha d - \frac{d m s}{m+t} \right)} \left(m^{\alpha d} r^{\frac{r t}{m+t} d} g^{\frac{-\omega(r+s)m'}{\omega(m+t)m'} d} y^d \right)^{-m'r'} g^{\left(\frac{m s}{\omega(m+t)m'} d - \frac{\alpha d}{\omega m'} - \frac{1}{m'} \right) (-m'r')} \\
&= m^{\left(\alpha d - \frac{d m s}{m+y} \right) m'r'} \left(m^{\alpha d} r^{\frac{r t}{m+t} d} g^{\frac{-r+s}{m+t} d} y^d \right)^{-m'r'} g^{\left(\frac{\alpha d}{\omega} - \frac{d m s}{\omega(m+t)} + 1 \right) r'} \\
&= \underbrace{\left(m^{m s} r^{r t} g^{-(r+s)} y^{m+t} \right)^{-d \frac{m'r'}{m+t}}}_{=1} g^{r' + \frac{d r'}{\omega} \left(\alpha - \frac{m s}{m+t} \right)} = g^{r'+s''} \pmod{p} .
\end{aligned}$$

For the final rewriting use the expression (3) for s' . According to step (7) of Figure 2, Bob produces terminated pairs because $t' = -m'$. This guarantees $t' \neq 0 \pmod{q}$ because m' is presumed not to disappear modulo q . The signature component r' does not disappear modulo q because of the loop condition in step (5).

Restrictiveness: First consider private key related attacks. Consider a polynomial-time attacker who has obtained $n \in \mathbb{IN}$ valid pairs $(m_i, (r_i, s_i, t_i))$ of messages and signatures for $i = 1, \dots, n$ from the signer. The signer has chosen $r_i = m_i^{a_i} g^{b_i} \pmod{p}$, and has computed the signature components s_i, t_i according to Figure 1. The signature components r_i release no information about the choices a_i, b_i to a polynomial-time attacker, so we need to look only at s_i and t_i .

According to Figure 1, $s_i = \frac{a_i r_i}{m_i} t_i$, which reveals the signer's choices a_i . From the t_i , the attacker learns the following system (4) of n linear equations over \mathbb{ZZ}_q in $n+1$ variables, namely b_i, x for $i=1, \dots, n$:

$$\begin{aligned}
m_i(r_i - m_i x) &= t_i(a_i r_i + b_i m_i r_i + m_i x) \\
\Leftrightarrow b_i m_i r_i t_i + m_i x(t_i + m_i) &= m_i r_i - a_i r_i t_i .
\end{aligned} \tag{4}$$

The values x and b_i are undetermined because $t_i, m_i \neq 0$, and therefore valid signatures release no more information about $x = \log_g y$ to a polynomial-time attacker, than y itself.

- 5 Next, show that an attacker who has not received any valid RUST signature with respect to a public key y cannot feasibly fabricate a valid signature for any message on his own (Case 0). An attacker who has got valid signatures for one or more messages m_i is considered afterwards (Case 1).

10 **Case 0:** By contradiction to restrictiveness (Definition 1), assume an attacker who has no valid pairs of messages and signatures in the first place ($n = 0$ in Definition 1), but succeeds to come up with a message m for which he has a witness $\omega \in \Omega$ that makes m , i.e., $m = g_1^\omega$, and a valid signature σ . (For lack of input pairs to *trans*, plain identifiers are used for the outputs, i.e., no primes.) According to Assumption A2, the attacker uses 3 parameters $a, c, d \in \mathbb{Z}\mathbb{Z}_q$ in order to build the signature component:

$$r = m^{a'} g^{c'} y^{d'} \bmod p .$$

15 Because m must be chosen to be g_1^ω , the only elements of G_q an attacker might use successfully to build r are those occurring in the verification equation (1), namely m, g, y . Would he use any other independently chosen element $h \in G_q$ and succeed to find a valid
20 signature, then the verification equation would reveal a representation of h with respect to m, g, y , which contradicts the discrete logarithm assumption.

Inserting the expression for r into the verification equation (1) yields:

$$g^{r+s} = y^{m+t} m^{ms} r^{rt} = y^{m+t} m^{ms} (m^{a'} g^{c'} y^{d'})^{rt} = y^{m+t} g_1^{\omega ms} (g_1^{\omega a'} g^{c'} y^{d'})^{rt} ,$$

which can be rewritten as:

$$g^{r+s-c't} = y^{m+t+d'rt} g_1^{\omega} (ns+a't) .$$

Since the bases g , y and g_1 are chosen independently, the only feasible way for the attacker to solve (5) is by letting the exponents of g , y and g_1 disappear.

5 This leads to the following linear system (6) of 3 equations in 2 variables s and t , over $\mathbb{Z}\mathbb{Z}_q$:

$$\begin{aligned} \omega m s + \omega a' r t &= 0 \\ -s + c' r t &= r \\ + (d' r + 1) t &= -m \end{aligned} \quad (6)$$

This system can be solvable only if the corresponding 3×3 determinant disappears:

$$\begin{vmatrix} \omega m & \omega a' r & 0 \\ -1 & c' r & r \\ 0 & d' r + 1 - m \end{vmatrix} = ((1 + a' + c' m) + d' r) \omega m r = 0 \quad (7)$$

10 Since neither ω nor m nor r may disappear modulo q , this condition (7) can be met only if $(1 + a' + c' m) + d' r = 0$. Here, the factors m and r are determined only after ω respective a' , c' , d' have been chosen, and by Assumption A1, neither m nor r can be predicted or coerced to any particular value. Hence the only way to let the determinant (7) disappear is to let $1 + a' + c' m = d' = 0 \pmod{q}$. However, protocol *trans* ensures with overwhelming probability that a dishonest Bob ends up with a representation of r whose exponent d' of y is not disappearing regardless of how Bob chooses r^* . Note that Bob must provide r^* before the Verifier sends his d and forms the signature component $r = (r^* y)^d g^{-1/m}$ in step (5).

20 **Case 1:** Due to the degenerate equivalence \equiv of witnesses, i.e., any two witnesses are equivalent, restrictiveness is satisfied whenever the attacker has obtained at least one valid pair (m, σ) and comes up with a new pair (m', σ') and a witness making m' . Restrictiveness requires no more, and thus nothing needs to be shown.

25 **Blindness:** Show that for each fresh valid pair (m, σ) , where $t \neq -m \pmod{q}$, and each terminated valid pair (m', σ') , where $t' = -m' \pmod{q}$, of messages and RUST signatures, and each choice $d \in \mathbb{Z}\mathbb{Z}_q^*$ of the verifier in *trans*, there is exactly one input $\omega \in \mathbb{Z}\mathbb{Z}_q^*$ and one value

$\alpha \in \mathbb{Z}\mathbb{Z}_q^*$ such that *trans* maps (m, σ) to (m', σ') . (Note that the value r^* of the verifier's view on Bob in *trans* is a one-to-one map of the other elements d, m', r' of his view, and thus from an information theoretic viewpoint, it suffices to consider d, m', σ' as the verifier's view.) In the following, all steps refer to protocol *trans* in Figure 2.

- 5 First show there is at most one pair (α, ω) : It is immediate from step (2) that the blinder $\omega = \log_m m'$ is uniquely determined. Furthermore, for each $d \in \mathbb{Z}\mathbb{Z}_q^*$ is obtained from steps (7), (6) and (3) in turn the following expression for s' :

$$s' = \frac{art - bms}{\omega rt} r' = \frac{\alpha d r t - \beta d m s}{\omega r t} r' = \frac{\alpha r t - \frac{rt}{m+t} ms}{\omega d r t} r' \pmod{q} .$$

10 Since all $r, t, d, r', (m+t)$ are presumed not to disappear modulo q , the internal choice α of Bob is uniquely determined as follows:

$$\alpha = \frac{\omega s'}{d r'} + \frac{ms}{m+t} \pmod{q} . \quad (8)$$

15 Next show that the uniquely determined pair (α, ω) from above transforms a fresh valid pair (m, σ) of message and signature into a terminated valid pair (m', σ') . Since $(m, \sigma) = (m, (r, s, t))$ is presumed a fresh valid pair, we can rewrite the verification equation (1) for $(m, (r, s, t))$ as follows:

$$\begin{aligned} g^{r+s} &= pk^{m+t} m^{ms} r^{rt} \\ \Leftrightarrow r^{rt} &= g^{r+s} pk^{-(m+t)} m^{-ms} , \text{ where } t \neq -m \pmod{q} . \end{aligned} \quad (9)$$

- 20 Furthermore, the unique α in equation (8) also determines a unique Υ in step (3), namely:

$$\begin{aligned}\gamma &= \frac{ms - \omega(r+s)m'}{\omega(m+t)m'} - \frac{\alpha}{\omega m'} = \frac{ms - \omega(r+s)m'}{\omega(m+t)m'} - \left(\frac{s'}{dm'r'} + \frac{ms}{\omega m'(m+t)} \right) \\ &= -\left(\frac{r+s}{m+t} + \frac{s'}{dm'r'} \right) \pmod{q} .\end{aligned}$$

Next, evaluate r' according to step (3) by inserting r^{rt} from equation (9), α from equation (8), $\beta = rt/(m+t)$ from step (3) and γ from equation (10):

$$\begin{aligned}r' &= (r * pk)^d g^{\frac{1}{m'}} \\ &= (m^\alpha r^\beta g^\gamma pk)^d g^{\frac{1}{m'}} \\ &= m^{\alpha d} r^{\frac{rt}{m+t}d} g^{\gamma d - \frac{1}{m'}} pk^d \\ &= m^{\alpha d} (g^{r+s} pk^{-(m+t)} m^{-ms})^{\frac{d}{m+t}} g^{\gamma d - \frac{1}{m'}} pk^d \\ &= m^{(\frac{\omega s'}{dr'} + \frac{ms}{m+t})d} (g^{r+s} m^{-ms})^{\frac{d}{m+t}} g^{-\left(\frac{r+s}{m+t} + \frac{s'}{dm'r'}\right)d - \frac{1}{m'}} \\ &= m^{\frac{\omega s'}{r'} - \frac{s'}{m'r'} - \frac{1}{m'}} g^{\frac{s'}{m'r'} - \frac{s'+r'}{m'r'}} \pmod{p} .\end{aligned}\tag{11}$$

- 5 Finally, check that the values m', r', s', t' satisfy the verification equation (1) if r' is inserted from (11) and use $t' = -m' \bmod q$ from step (7):

$$pk^{m'+t'} m'^{m's'} r'^{r't'} = pk^{m'-m'} m'^{m's'} (m'^{\frac{s'}{r'}} g^{\frac{s'+r'}{m'r'}})^{-r'm'} = g^{r'+s'} \pmod{p} .$$

This concludes the proof.

A restrictive blind signature scheme has been presented that allows a recipient to obtain signatures for arbitrarily many (correctly formed) messages after only one interaction with the
 5 signer. Signing, transforming and verifying costs two, six, and six full length modular exponentiations, respectively. For transforming and verifying, count the exponentiations of Bob and of the Verifier in *trans*, respectively. This compares to two, five and four modular exponentiations of the signer and recipient during the signing protocol and verification of the one-time restrictive blind signature protocol proposed by Chaum, Pedersen [CP92] and later by
 10 Brands [B93].

Various illustrative examples of the invention have been described in detail. In addition, however, many modifications and changes can be made to these examples without departing from the nature and spirit of the invention.

References

- 15 [BBS98] Matt Blaze, Gerrit Bleumer, Martin Strauss: Divertible Protocols and Atomic Proxy Cryptography; Eurocrypt '98, LNCS 1403, Springer-Verlag, Berlin 1998, 127-144.
- [B98] Gerrit Bleumer: Biometric yet Privacy Protecting Person Authentication; Information Hiding Workshop '98, LNCS 1525, Springer-Verlag, Berlin 1998,
 20 101-112.
- [B99] Gerrit Bleumer: Biometric Authentication and Multilateral Security; in Günter Müller, Kai Rannenberg (Eds.): Multilateral Security for Global Communication.
- [BR93] Mihir Bellare, Phillip Rogaway: Random Oracles are Practical: A Paradigm for Designing Efficient Protocols; 1st ACM Conference on Computer and
 25 Communications Security, Proceedings, Fairfax, November 1993, ACM Press, New York 1993, 62-73.
- [B93] Stefan Brands: An Efficient Off-line Electronic Cash System Based On The Representation Problem; Centrum voor Wiskunde en Informatica, Computer Science/Departement of Algorithmics and Architecture, Report CS-R9323, March
 30 1993.

- [B94] Stefan Brands: Untraceable Off-line Cash in Wallet with Observers; Crypto '93, LNCS 773, Springer-Verlag, Berlin 1994, 302-318.
- [BGK95] Ernest Brickell, Peter Gemmell, David Kravitz: Trustee-based racing Extensions to Anonymous Cash and the Making of Anonymous Change; 6th ACM-SIAM Symposium on Discrete Algorithms (SODA)1995, ACM Press, New York 1995, 457-466.
- [BS96] Eric Bach, Jeffrey Shallit: Algorithmic Number Theory, Vol. 1; MI Press, Cambridge MA 1996.
- [C83] David Chaum: Blind Signature System; Crypto '83, Plenum Press, New York 1984, 153.
- [C84] David Chaum: A New Paradigm for Individuals in the Information Age; 1984 IEEE Symposium on Security and Privacy, IEEE Computer Society Press, Washington 1984, 99-103.
- [C85] David Chaum: Security without Identification: Transaction Systems to make Big Brother Obsolete; Communications of the ACM 28/10 (1985)1030-1044.
- [C88] David Chaum: Card-Computer Moderated Systems; United States Patent, Patent Number 4,926,480, Date of Patent 15.05.1990.
- [C90] David Chaum: Showing credentials without identification: Transferring signatures between unconditionally unlinkable pseudonyms; Auscrypt '90, LNCS 453, Springer-Verlag, Berlin 1990, 246-264.
- [CFN90] David Chaum, Amos Fiat, Moni Naor: Untraceable Electronic Cash; Crypto '88, LNCS 403, Springer-Verlag, Berlin 1990, 319-327.
- [CP92] David Chaum, Torben Pryds Pedersen: Wallet Databases with Observers. Crypto '92, LNCS 740, Springer-Verlag, Berlin 1993, 89-105.
- [CPS94] Jan L. Camenisch, Jean-Marc Piveteau, Markus A. Stadler: An Efficient Electronic Payment System Protecting Privacy; ESORICS 94 (Third European Symposium on Research in Computer Security), Brighton, LNCS 875, Springer-Verlag, Berlin 1994, 207-215.
- [CPS95] Jan L. Camenisch, Jean-Marc Piveteau, Markus A. Stadler: Blind Signatures Based on the Discrete Logarithm Problem; Eurocrypt '94, LNCS 950, Springer-Verlag, Berlin 1995, 428-432.
- [CPS96] Jan L. Camenisch, Jean-Marc Piveteau, Markus A. Stadler: An Efficient Fair Payment System; 3rd ACM Conference on Computer and Communications Security, New Delhi, India, March 1996, ACM Press, New York 1996, 88-94.
- [EG85] Taher ElGamal: A Public Key Cryptosystem and a Signature Scheme Based on Discrete Logarithms; IEEE Transactions on Information Theory 31/4 (1985)469-472.
- [F94] Niels Ferguson: Single Term Off-Line Coins; Eurocrypt '93, LNCS 765, Springer-Verlag, Berlin 1994, 318-328.

- [FS87] Amos Fiat, Adi Shamir: How to Prove Yourself: Practical Solutions to Identification and Signature Problems; Crypto 86, LNCS 263, Springer-Verlag, Berlin 1987, 186-194.
- 5 [F Y96] Yair Frankel, Yiannis Tsiounis, Moti Yung: "Indirect Discourse Proofs": Achieving Efficient Fair Off-Line E-cash; Asia crypt '96, LNCS 1163, Springer-Verlag, Berlin 1996, 286-300.
- [FY93] Matthew Franklin, Moti Yung: Secure and Efficient Off-Line Digital Money; 20th International Colloquium on Automata, Languages and Programming (ICALP), LNCS 700, Springer-Verlag, Berlin 1993, 265-276.
- 10 [GMR88] Shafi Goldwasser, Silvio Micali, Ronald L. Rivest: A Digital Signature Scheme Secure Against Adaptive Chosen-Message Attacks; SIAM Journal on Computing 17/2 (1988)281-308.
- [MOV97] Alfred J. Menezes, Paul C. van Oorschot, Scott A. Vanstone: Handbook of Applied Cryptography; CRC Press, Boca Raton 1997.
- 15 [NIS 93] National Institute of Standards and Technology: Digital Signature Standard; Federal Information Processing Standards Publication (FIPS PUB xx), February 1, 1993.
- [O99] Andrew M. Odlyzko: Designs, Codes, and Cryptography (1999). To appear. <http://www.research.att.com/amo/doc/complete.html>
- 20 [PS97] David Pointcheval, Jacques Stern: Provably Secure Blind Signature Schemes; Asiacrypt '96, LNCS 1163, Springer-Verlag, Berlin 1996, 252-265.
- [PS97a] David Pointcheval, Jacques Stern: New Blind Signatures Equivalent to Factorization; 4th ACM Conference on Computer and Communications Security, ACM-Press, New York 1997, 92-99.
- 25 [PS99] Birgit Pfitzmann, Ahmad-Reza Sadeghi: Coin-Based Anonymous Fingerprinting; To appear at Eurocrypt '99, Springer-Verlag, Berlin 1999.
- [RGV97] Cristian Radu, Ren Govaerts, Joos Vandewalle: Efficient electronic cash with restricted privacy; Financial Cryptography '97, Springer-Verlag, Berlin, 57-69.
- 30 [RGV96] C. Radu, R. Govaerts, J. Vandewalle: A Restrictive Blind Signature Scheme with Applications to Electronic Cash; 2nd IFIP Communications and Multimedia Security, Chapman & Hall, London 1996, 196-207.
- [SPC95] Markus Stadler, Jean-Marc Piveteau, Jan Camenisch: Fair Blind Signatures; Eurocrypt '95, LNCS 921, Springer-Verlag, Berlin 1995, 209-219.

CLAIMS

What is claimed is:

- 5 1. A multiple use ticket method, comprising:

providing a blind signature in a ticket, the signature having a multiple use; and

developing a blinding value for the signature in a reproducible computation using a seed key

substantially known only to the issuer of the ticket.
- 10 2. The method of claim 1 wherein said signature has a built-in expiration.
- 15 3. The method of claim 1 wherein said ticket is an electronic personal ticket.
- 20 4. The method of claim 1 wherein said ticket is an electronic season ticket.
- 25 5. The method of claim 1 wherein said ticket is an untraceable electronic personal
ticket.
6. The method of claim 1 wherein said ticket is a personal license.
7. The method of claim 1 wherein said ticket is a personal driver's license.
- 30 8 The method of claim 1 wherein said signature does not require an interactive
signing protocol.
9. The method of claim 1 wherein said ticket is an offline personal ticket.
- 35 10. A system for generating a multiple use ticket method, comprising:

means for providing a blind signature in a ticket, the signature having a multiple use; and
means for developing a blinding value for the signature in a reproducible computation
using a seed key substantially known only to the issuer of the ticket.

5

11. The system of claim 10, wherein said signature has a built-in expiration.

10

12. An article of manufacture for a computer system, for providing a multiple use
ticket, comprising:

a computer readable medium;

computer code in said computer readable medium for providing a blind signature in a
ticket, the signature having a multiple use; and

15

computer code in said computer readable medium for providing a blinding value for the
signature in a reproducible computation using a seed key substantially known only to the issuer
of the ticket.

20

13. The article of manufacture of claim 12, wherein said signature has a built-in
expiration.

ABSTRACT OF THE DISCLOSURE

A multiple use ticket generating method is disclosed which enables a recipient to obtain signatures for arbitrarily many (correctly formed) messages after only one interaction with the signer. The method provides a blind signature in a ticket, the signature having a multiple use with a built-in expiration. Then, the method develops a blinding value for the signature in a reproducible computation using a seed key substantially known only to the issuer of the ticket. The method implements a new class of signature schemes almost as efficiently as do previous one-time restrictive blind signature methods.

10

Docket 2455-4581US1

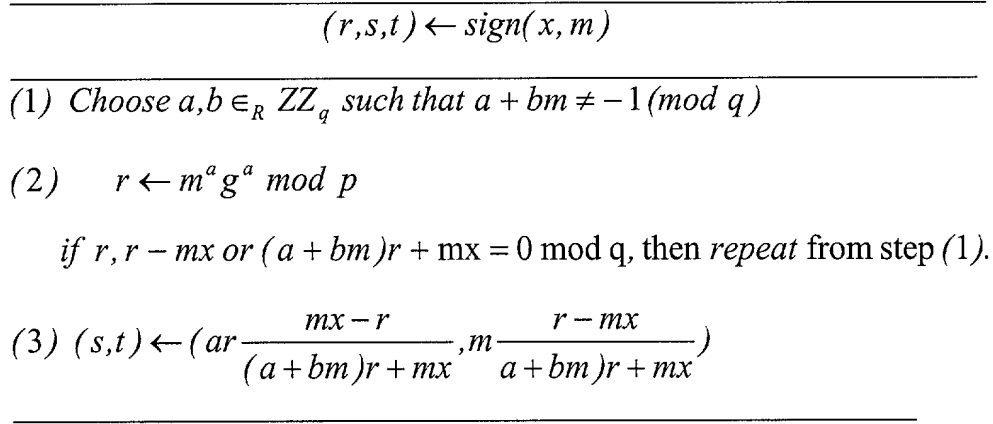


Fig. 1. Producing a signature

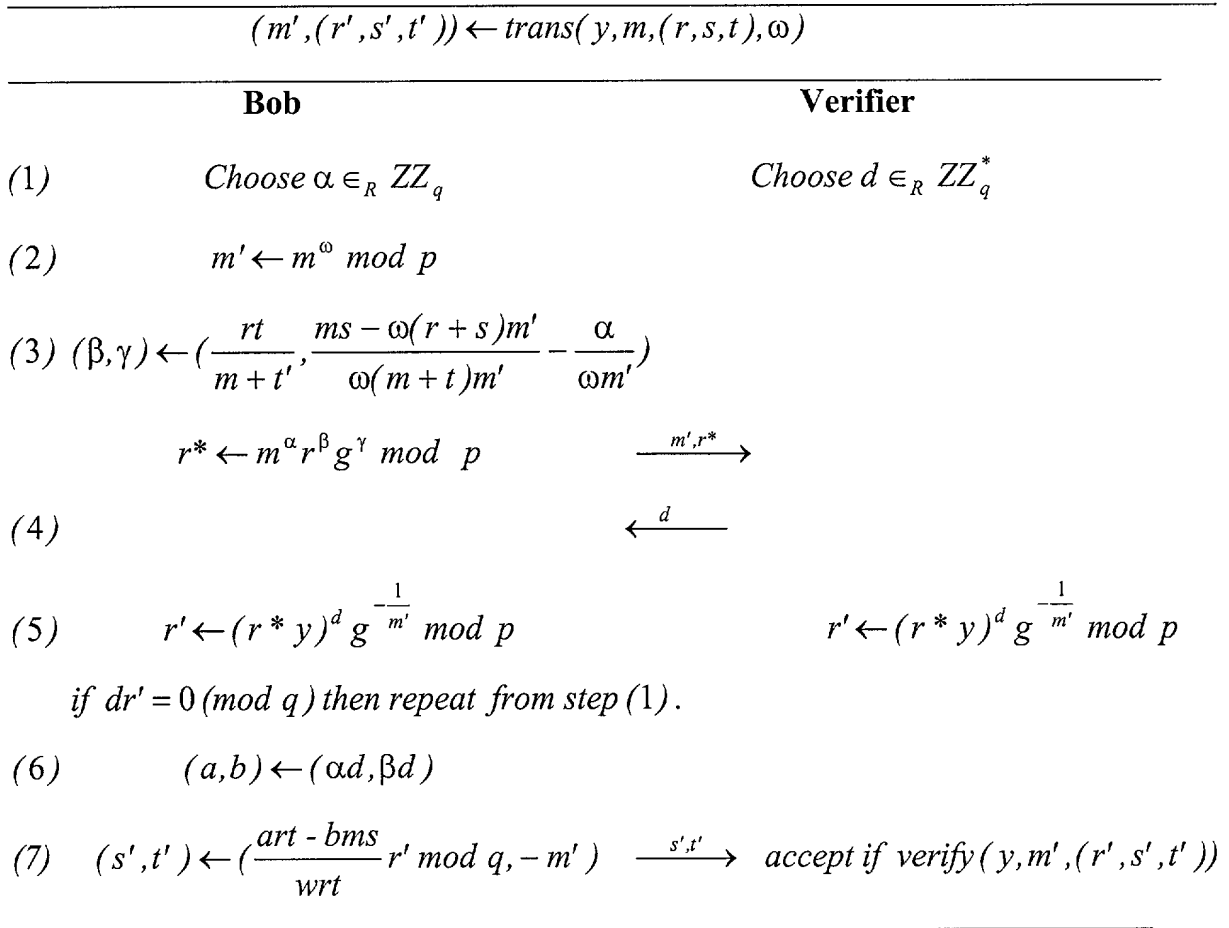


Fig. 2. Transforming a signature

IN THE UNITED STATES
PATENT AND TRADEMARK OFFICE

Declaration and Power of Attorney

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name.

I believe I am an original, first and sole inventor of the subject matter which is claimed and for which a patent is sought on the invention entitled **METHOD FOR GENERATING MANY-TIME RESTRICTIVE BLIND SIGNATURES**, the specification of which ☒ is attached hereto ☐ was filed on _____ as U.S. Serial No. _____

I hereby state that I have reviewed and understand the contents of the above identified specification, including the claims, as amended by an amendment, if any, specifically referred to in this oath or declaration.

I acknowledge the duty to disclose all information known to me which is material to patentability as defined in Title 37, Code of Federal Regulations, 1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, 119 of any foreign application(s) for patent or inventors' certificate listed below and have also identified below any foreign application for patent or inventors' certificate having a filing date before that of the application on which priority is claimed:

I hereby claim the benefit under Title 35, United States Code, 120 of any United States application(s) listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States application in the manner provided by the first paragraph of Title 35, United States Code, 112, we acknowledge the duty to disclose all information known to us to be material to patentability as defined in Title 37, Code of Federal Regulations, 1.56 which became available between the filing date of the prior application and the national or PCT international filing date of this application:

U.S. Serial No. 60/161,062, filed October 25, 1999

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

I hereby appoint the following attorney(s) with full power of substitution and revocation, to prosecute said application, to make alterations and amendments therein, to receive the patent, and to transact all business in the Patent and Trademark Office connected therewith:

Samuel H. Dworetsky (Reg. No. 27873)
Thomas A. Restaino (Reg. No. 33444)
Michele L. Conover (Reg. No. 34962)
Benjamin S. Lee (Reg. No. 42787)
Robert B. Levy (Reg. No. 28234)
Alfred G. Steinmetz (Reg. No. 22971)
Cedric G. DeLaCruz (Reg. No. 36498)
Rohini K. Garg (Reg. No. 45272)
Susan E. McHale (Reg. No. 35948)
Thomas M. Isaacson (Reg. No. 44166)
Gary H. Monka (Reg. No. 35290)
Jeffrey M. Navon (Reg. No. 32711)

I also appoint Christopher A. Hughes (Reg. No. 36,914), John E. Hoel (Reg. No. 26,279) and Joseph C. Redmond (Reg. No. 18,753) of Morgan & Finnegan as associate attorneys, with full power to prosecute said application, to make alterations and amendments therein, and to transact all business in the U.S. Patent and Trademark Office connected therewith.

Please address all correspondence to Morgan & Finnegan, L.L.P., 345 Park Avenue, New York, NY 10154-0053. Telephone calls should be made to (202)-857-8011.

Full name of first or sole inventor: Gerrit Bleumer

Inventor's signature _____ Date _____

Residence: Beethovenweg 15, 16727 Velten GERMANY

Citizenship: German

Post Office Address: Beethovenweg 15, 16727 Velten GERMANY